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DYNAMIC RESPONSE ANALYSIS OF SUBMERGED SOIL

BY THIN LAYER ELEMENT METHOD

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A thin layer element method is formulated to compute the dynamic response of submerged soil. The formulation is based on Biot's equation describing the dynamic behavior of fluid-saturated elasto-porous medium. The dynamic response of submerged soil is computed for various cases by using the developed formulation. The effects of submerged conditions are examined for submerged soil deposits with a water level at and above the ground surface. It is found that both submerged conditions and water body above the ground surface can considerably affect the dynamic response of soil deposits.

INTRODUCTION

When the dynamic load is applied to saturated soil, pore fluid movement relative to the soil skeleton may be induced. The transient movement and redistribution of pore fluid can significantly affect the dynamic response soil behavior. They are generally governed by the loading rate, soil permeability, pressure gradient and boundary conditions, resulting in an extremely complex picture of the dynamic response behavior of submerged soil.

Biot (1962) has made a framework in the formulation of dynamic response of fluid-filled elasto-porous medium. This formulation has been generally used for dynamic response analysis of submerged soil and evaluated typically by either analytical solutions obtained by solving the differential equations or the numerical finite element method.

Considerable difficulty exists in obtaining analytical solutions for Biot's equation in general and thus the solutions have been developed only for very simple conditions (e.g. Biot, 1956; Jones, 1961; Deresiewics, 1960; Foda and Mei, 1982). Those conditions are generally too simple compared with those commonly encountered in the real situation.

The finite element method has been applied for the numerical evaluation of Biot's equation (e.g. Ghaboussi and Wilson, 1973; Prevost, 1982; Simon et al., 1986; Zienkiewicz et al., 1977). Contrary to the former approach, this approach can account for complex geometry

and inhomogeneity without increasing the degree of difficulty and amount of computation. However, compared with the finite element scheme applied to a single-phase medium, the computation effort increases substantially due to the additional degrees of freedom associated with pore fluid. Various people (e.g. Kausel and Roesset, 1975; Lysmer and Waas, 1972; and Tajimi and Shimomura, 1976) have presented a thin layer element method, which combines the finite element scheme and analytical solution and uses the Rayleigh wave modes in the expression of the responses. This approach requires computation effort far less than the regular finite element approach and yet has a capacity of accommodating complex conditions far more than the approach with the analytical solution. It has been applied to the dynamic response computation of a single-phase medium but does not appear to have been applied to a fluid-saturated porous medium in published literature. For the dynamic response analysis of a two-phase mixture, this approach appears to be very attractive because a large computation effort is generally required in such analysis by the regular finite element method.

FORMULATION

The soil medium is assumed to be an elastic porous medium saturated with pore fluid. The average displacement of the pore fluid relative to the displacement of the solid skeleton is defined as

$$\mathbf{w} = \mathbf{n}(\mathbf{U} - \mathbf{u}) \tag{1}$$

where n = porosity; $\mathbf{w} = (\mathbf{w}_x, \mathbf{w}_z)^T$ in which \mathbf{w}_j is relative displacement of fluid in the j direction; $\mathbf{u} = (\mathbf{u}_x, \mathbf{u}_z)^T$ in which \mathbf{u}_j is displacements of solid skeleton in the j direction; $\mathbf{U} = (\mathbf{U}_x, \mathbf{U}_z)^T$ in which \mathbf{U}_j is the absolute displacement of the fluid in the j direction; and x and z = Cartesian coordinates in horizontal and vertical directions, respectively. The total normal stresses acting on a unit area of mixture is

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$$\mathbf{\sigma} = (1-n)\mathbf{\sigma}_{s} + mn\pi = \mathbf{\sigma}^{t} + m\pi \tag{2}$$

where $\sigma_s = (\sigma_{sx}, \, \sigma_{sz}, \, \tau_{xz})^T$ in which σ_{sj} is a normal stress in the j direction acting on the solid skeleton over the unit area; $\sigma = (\sigma_x, \, \sigma_y, \, \tau_{xz})^T$ in which σ_j is a total normal stress in the j direction; $\sigma' = (\sigma_x', \, \sigma_z', \, \tau_{xz})^T$ in which σ_j' is an effective normal stress in the j direction; τ_{xz} = shear stress; π = pore fluid pressure; and $\mathbf{m} = (1,1,0)^T$.

The equilibrium condition of forces acting on the soil skeleton in a unit soil volume is described as

$$(1-n)\mathbf{L}^{\mathsf{T}}\sigma_{s} + (1-n)\rho_{s}\mathbf{b} + n\mathbf{k}^{-1}\dot{\mathbf{w}} = (1-n)\rho_{s}\dot{\mathbf{u}}$$
(3)

where $\dot{\mathbf{w}} = \partial \mathbf{w}/\partial t$; $\dot{\mathbf{u}} = \partial^2 \mathbf{u}/\partial t^2$; $\mathbf{b} = (b_x, b_z)^T$ in which b_j is body force in the j direction per unit mass; ρ_s = density of a unit volume of the solid material in the skeleton; and

$$\mathbf{L}^{\mathsf{T}} = \begin{bmatrix} \frac{\partial}{\partial \mathbf{x}} & 0 & \frac{\partial}{\partial \mathbf{z}} \\ 0 & \frac{\partial}{\partial \mathbf{z}} & \frac{\partial}{\partial \mathbf{x}} \end{bmatrix} \tag{4}$$

The equilibrium condition of the forces acting on the pore fluid domain in a unit volume of soil is given by

$$n\nabla\pi - k^{-1}n\dot{w} + n\rho_{f}b = \rho_{f}\dot{w} + n\rho_{f}\dot{u}$$
 (5)

where ρ_f = density of unit volume of pore fluid; and $\nabla = (\partial/\partial x, \partial/\partial z)^T$. Combining Eqs. 3 and 5, the equilibrium condition of the pore fluid and solid skeleton mixture is expressed as

$$\mathbf{L}^{\mathsf{T}}\boldsymbol{\sigma} + \rho \mathbf{b} = \rho \ddot{\mathbf{u}} + \rho_{\mathsf{f}} \ddot{\mathbf{w}} \tag{6}$$

where ρ = density of unit volume of mixture = $(1-n)\rho_s + n\rho_f$. Since linear elastic conditions are considered, body forces will be neglected hereafter.

The rate of the fluid stored in a unit volume mixture is equal to the summation of the rate of the volume change of volumetric strain in the solid, the rate of change due to compression of the solid by pore fluid pressure, the rate of change due to compression of the solid by the effective stresses, and the rate of change due to compressibility of the fluid. According to Simon et al. (1984), this is expressed as

$$\nabla^{\mathsf{T}}\mathbf{w} = -\alpha\mathbf{m}^{\mathsf{T}}\mathbf{\varepsilon} + \mathbf{O}^{\mathsf{T}}\mathbf{\pi} \tag{7}$$

where $\boldsymbol{\varepsilon} = \text{strains} = (\varepsilon_x, \varepsilon_z, \gamma_{xz})^T$; and α and Q are related with material properties through

$$\alpha = 1 - \frac{K_d}{K_s}$$
 and $Q^{-1} = \frac{1}{K_f} + \frac{\alpha - n}{K_s}$ (8)

where K_s = elastic volumetric modulus of solid; K_f = volumetric modulus of fluid; and K_d = elastic volumetric modulus of solid skeleton. Substituting π in Eq. 7 into Eq. 2 and using the stress-strain relationship, $\sigma' = D\epsilon$, the total stresses, σ , can be correlated with ϵ and \mathbf{w} . With $\epsilon = \mathbf{L}\mathbf{u}$, this expression and pore fluid pressure given in Eq. 7 can be written in a matrix form such that

$$\begin{cases} \mathbf{0} \\ \mathbf{\pi} \end{cases} = \begin{bmatrix} (\mathbf{D} + \alpha^2 \mathbf{Q} \mathbf{m} \mathbf{m}^T) \mathbf{L} & \alpha \mathbf{Q} \mathbf{m} \nabla^T \\ \alpha \mathbf{Q} \mathbf{m}^T \mathbf{L} & \mathbf{Q} \nabla^T \end{bmatrix} \mathbf{u} \\ \mathbf{w} \end{cases}$$
(9)

Using π and σ defined in Eq. 9, Eqs. 5 and 6 can be rewritten in the following matrix form after using the relationship $\varepsilon = Lu$:

$$-\mathbf{M} \begin{bmatrix} \dot{\mathbf{u}} \\ \dot{\mathbf{w}} \end{bmatrix} - \mathbf{C} \begin{bmatrix} \dot{\mathbf{u}} \\ \dot{\mathbf{w}} \end{bmatrix} + \mathbf{K} \begin{bmatrix} \mathbf{u} \\ \mathbf{w} \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}$$
 (10)

where

$$\mathbf{M} = \begin{bmatrix} \rho & \rho_{f} \\ \rho_{f} & \rho_{f} / n \end{bmatrix} \qquad \mathbf{C} = \begin{bmatrix} 0 & 0 \\ 0 & k^{-1} \end{bmatrix} \qquad \mathbf{K} = \begin{bmatrix} \mathbf{L}^{T} (\mathbf{D} + \alpha^{2} \mathbf{Q} \mathbf{m} \mathbf{m}^{T}) \mathbf{L} & \alpha \mathbf{Q} \mathbf{L}^{T} \mathbf{m} \nabla^{T} \\ \alpha \mathbf{Q} \nabla \mathbf{m}^{T} \mathbf{L} & \mathbf{Q} \nabla \nabla^{T} \end{bmatrix}$$
(11)

Consider a horizontally layered submerged soil. The displacements of the medium in the wave field is expressed in the form of $(\mathbf{u}(x,z,t),\mathbf{w}(x,z,t))=(\mathbf{u}(x),\mathbf{w}(z))\mathrm{e}^{-\mathrm{i}(\omega t-hx)}$ in which $\omega=$ circular frequency and h= wave number. Using a shape function in the z direction and omitting the time facor, the displacements of the jth layer in the wave field are approximately expressed by using the displacements at the upper and lower ends of the jth layer as

$${\mathbf{u}_{j}(\mathbf{x},\mathbf{z}) \atop \mathbf{w}_{i}(\mathbf{x},\mathbf{z})} = e^{-ih\mathbf{x}} \mathbf{Z}(\mathbf{z}) {\mathbf{U}_{j} \atop \mathbf{W}_{j}}$$
 (12)

where e^{-ihx} $U_j^T = (u_j(x,0)^T, u_j(x,H_j)^T)$ and e^{ihx} $W_j^T = (w_j(x,0)^T, w_j(x,H_j)^T)$, in which z=0 and H_j indicate respectively the upper end and lower ends of the jth layer; ; and Z(z) = matrix containing the shape function . When linear variations of the displacements are assumed along z, the shape function matrix Z is

$$\mathbf{Z}(z) = \left(1 - \frac{z}{H_j}, \frac{z}{H_j}\right)\mathbf{I}$$
 (13)

where I = 4x4 identity matrix. It is noted in Eq. 13 that the factor $(1-z/H_j, z/H_j)$ is simply multiplied by the numbers in I and thus Z is a matrix with 4 rows and 8 columns.

After substituting Eq. 12 into Eq. 10, application of Galarkin's procedure to Eq. 10 results in

 $\sum_{i=1}^{J} \int_{V} \mathbf{Z}^{T} \left(\mathbf{K}_{j} - i\omega \mathbf{C}_{j} + \omega^{2} \mathbf{M}_{j} \right) \mathbf{Z} \left\{ \mathbf{W}_{j}^{U} \right\} e^{-ihx} dV \sum_{i=1}^{J} \int_{S} \mathbf{Z}^{T} \mathbf{K}_{j}' \mathbf{Z} \begin{Bmatrix} \mathbf{U}_{j} \\ \mathbf{W}_{j} \end{Bmatrix} e^{-ihx} dS = \mathbf{0}$

(14)

where J = numbers of layers; V = volume of the layer j; S = surface area of the layer j; and $K' = \int K dz$. Transforming the surface integration in Eq. 14 into the volume integration and integrating over x result in

$$\sum_{j=1}^{J} \int_{0}^{H_{j}} \left\{ \mathbf{Z}^{\mathsf{T}} \left(\mathbf{K}_{j} - i\omega \mathbf{C}_{j} + \omega^{2} \mathbf{M}_{j} - \frac{\partial \mathbf{K}_{j}^{\mathsf{T}}}{\partial \mathbf{z}} \right) - \frac{\partial \mathbf{Z}^{\mathsf{T}}}{\partial \mathbf{z}} \mathbf{K}_{j}^{\mathsf{T}} \right\} \mathbf{Z} \left\{ \mathbf{W}_{j}^{\mathsf{T}} \right\} d\mathbf{z} = \mathbf{0}$$
(15)

Substituting Eq. 15 into Eq. 14 and performing integration with respect to z result in the characteristics equation in the discretized form such that

$$\sum_{j=1}^{J} \left(h^2 \boldsymbol{\alpha}_j + i h \boldsymbol{\beta}_j + \boldsymbol{\gamma}_j \right) \begin{Bmatrix} U_j \\ W_j \end{Bmatrix} = 0$$

or

$$\left(h^2 \mathbf{\alpha} + ih\mathbf{\beta} + \mathbf{\gamma}\right) \begin{Bmatrix} \mathbf{U} \\ \mathbf{W} \end{Bmatrix} = \mathbf{0} \tag{16}$$

where

$$\alpha_j = \frac{H_j}{6} \begin{bmatrix} Aa & 0a & \alpha Qa & 0a \\ 0a & Ga & 0a & 0a \\ \alpha Qa & 0a & Qa & 0a \\ 0a & 0a & 0a & 0a \end{bmatrix}$$

$$\mathbf{\beta}_{j} = \frac{1}{2} \begin{bmatrix} 0b & (A-2G)b & 0b & \alpha Qb \\ Gb & 0b & 0b & 0b \\ 0b & \alpha Qb & 0b & Qb \\ 0b & 0b & 0b & 0b \end{bmatrix}^{T} - \frac{1}{2} \begin{bmatrix} 0b & (A-2G)b & 0b & \alpha Qb \\ Gb & 0b & 0b & 0b \\ 0b & \alpha Qb & 0b & Qb \\ 0b & 0b & 0b & 0b \end{bmatrix}$$
(17)

in which $A = \lambda + 2G + \alpha^2Q$; and

$$\mathbf{a} = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix} \qquad \mathbf{b} = \begin{bmatrix} 1 & -1 \\ 1 & -1 \end{bmatrix} \qquad \mathbf{c} = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \tag{18}$$

Wave numbers, h, and their associated mode shape vectors, $(\phi_{\mathbf{u}}^{T}, \phi_{\mathbf{w}}^{T})^{T}$, can be determined by solving the characteristic equation Eq. 16. Since the fluid pressure is an all around equal pressure, there is a constraint between the freedoms associated with $w_{\mathbf{x}}$ and $w_{\mathbf{z}}$ and thus the total degree of freedoms for J layers is 3J instead of 4J. This results in 3J non-zero conjugate pairs and J zero conjugate pairs in eigenvalues computed from Eq. 16. In order to satisfy the wave scattering conditions, only those with the plus sign in the imaginary part are selected among the conjugate pairs. Then, the displacements of the submerged layered-soil is expressed along x at the nodal points as

and thus the displacements within the jth layer as

$$\begin{cases} \mathbf{u}_{j}(\mathbf{x}, \mathbf{z}) \\ \mathbf{w}_{i}(\mathbf{x}, \mathbf{z}) \end{cases} = \mathbf{Z}(\mathbf{z}) \sum_{s=1}^{3J} e^{-i\mathbf{h}_{s}\mathbf{x}} \alpha_{s} \begin{cases} \phi_{uj} \\ \phi_{wj} \end{cases}_{s}$$
 (19)

where $(\phi_{\mathbf{u}}^{\mathrm{T}}, \phi_{\mathbf{w}}^{\mathrm{T}})_{s}^{\mathrm{T}}$ = sth eigenvector in which $\phi_{\mathbf{u}}$ and $\phi_{\mathbf{w}}$ = vectors of size 2J; $\phi_{\mathbf{u}j}$ and $\phi_{\mathbf{w}j}$ = vectors containing the values at the locations corresponding the jth layer in $\phi_{\mathbf{u}}$ and $\phi_{\mathbf{w}}$, respectively; h_{s} = sth eigenvalue; and α_{s} = sth mode participation factor. Then, using Eqs. 9 and 19 together with Eq. 13, the stresses and pore fluid pressure at the middle of the jth layer are

$$\begin{cases}
\boldsymbol{\sigma}_{j}^{r}(x, 0.5H_{j}) \\
\boldsymbol{\pi}_{j}(x, 0.5H_{j})
\end{cases} = -i A_{j} \sum_{s=1}^{3J} h_{s} e^{-ih_{s}x} \alpha_{s} \begin{cases} \boldsymbol{\phi}_{uj} \\ \boldsymbol{\phi}_{wj} \end{cases}_{s} + B_{j} \sum_{s=1}^{3J} e^{-ih_{s}x} \alpha_{s} \begin{cases} \boldsymbol{\phi}_{uj} \\ \boldsymbol{\phi}_{wj} \end{cases}_{s} \tag{20}$$

where

$$A_{j} = \frac{1}{2} \begin{bmatrix} A & A & 0 & 0 & \alpha Q & \alpha Q & 0 & 0 \\ A-2G & A-2G & 0 & 0 & \alpha Q & \alpha Q & 0 & 0 \\ 0 & 0 & G & G & 0 & 0 & 0 & 0 \\ \alpha Q & \alpha Q & 0 & 0 & Q & Q & 0 & 0 \end{bmatrix}$$

$$B_{j} = \frac{1}{H_{j}} \begin{bmatrix} 0 & 0 - (A-2G) & (A-2G) & 0 & 0 & -\alpha Q & \alpha Q \\ 0 & 0 & -A & A & 0 & 0 & -\alpha Q & \alpha Q \\ -G & G & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\alpha Q & \alpha Q & 0 & 0 & -Q & Q \end{bmatrix}$$

$$(21)$$

A vertical cut is considered at x=0 in a layered soil. After substituting Eqs. 13 and 19 into Eq. 9, the nodal forces acting on the vertical cut of the jth layer for $x\ge0$ can be obtained as

$$\begin{Bmatrix}
\mathbf{P}_{\mathbf{z}j} \\
\mathbf{P}_{\mathbf{z}j} \\
\mathbf{P}_{\mathbf{\pi}j}
\end{Bmatrix} = \mathbf{i} \ \mathbf{E}_{j} \sum_{s=1}^{3J} \mathbf{h}_{s} \alpha_{s} \begin{Bmatrix} \mathbf{\phi}_{\mathbf{u}j} \\
\mathbf{\phi}_{\mathbf{w}\mathbf{x}j} \end{Bmatrix}_{s} + \mathbf{F}_{j} \sum_{s=1}^{3J} \alpha_{s} \begin{Bmatrix} \mathbf{\phi}_{\mathbf{u}j} \\
\mathbf{\phi}_{\mathbf{w}\mathbf{z}j} \end{Bmatrix}_{s}$$
(22)

where

$$\begin{cases}
\mathbf{P}_{xj} \\ \mathbf{P}_{zj} \\ \mathbf{P}_{\pi j}
\end{cases} = -\int_{0}^{H_{j}} \mathbf{N}^{T} \begin{Bmatrix} \mathbf{Q}_{xj}(0,z) \\ \mathbf{\tau}_{xzj}(0,z) \end{Bmatrix} dz$$

$$\mathbf{E}_{j} = \frac{H_{j}}{6} \begin{bmatrix} \mathbf{A}\mathbf{a} & \mathbf{0}\mathbf{a} & \alpha \mathbf{Q}\mathbf{a} \\ \mathbf{0}\mathbf{a} & \mathbf{G}\mathbf{a} & \mathbf{0}\mathbf{a} \\ \alpha \mathbf{Q}\mathbf{a} & \mathbf{0}\mathbf{a} & \mathbf{Q}\mathbf{a} \end{bmatrix} \quad \text{with} \quad \mathbf{a} = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$$

$$\mathbf{F}_{j} = \frac{1}{2} \begin{bmatrix} \mathbf{0}\mathbf{b} & (\mathbf{A}-2\mathbf{G})\mathbf{b} & \alpha \mathbf{Q}\mathbf{b} \\ \mathbf{0}\mathbf{b} & \mathbf{0}\mathbf{b} & \mathbf{0}\mathbf{b} \\ \mathbf{0}\mathbf{b} & \alpha \mathbf{b} & \mathbf{Q}\mathbf{b} \end{bmatrix} \quad \text{with} \quad \mathbf{b} = \begin{bmatrix} 1 & -1 \\ 1 & -1 \end{bmatrix}$$
(23)

Therefore those of the entire layered system for x≥0 are

$$\begin{cases}
P_x \\
P_z \\
P_\pi
\end{cases} = i E \sum_{s=1}^{3J} h_s \alpha_s \begin{cases} \phi_u \\ \phi_{wx} \end{cases}_s + F \sum_{s=1}^{3J} \alpha_s \begin{cases} \phi_u \\ \phi_{wz} \end{cases}_s$$

or

$$\begin{Bmatrix}
\mathbf{P}_{\mathbf{x}} \\
\mathbf{P}_{\mathbf{z}} \\
\mathbf{P}_{\pi}
\end{Bmatrix} = \left(i \mathbf{E} \mathbf{\phi}' + \mathbf{F} \mathbf{\phi}''\right) \mathbf{\alpha} \tag{24}$$

where ϕ' and $\phi'' = 3J \times 3J$ matrices containing the vectors $h_s(\phi_u^T, \phi_{wx}^T)_s^T$ and $(\phi_u^T, \phi_{wz}^T)_s^T$ at the sth column, respectively; and $\phi'' = v$ vector containing $\phi'' = v$ at the sth location. Given external loads at v = v, v = v, the participation factors, v = v, can be determined from Eq. 24 with v = v, v = v,

It is noted that , when the layer is made of fluid only, Eq. 10 and all other formulations can be rewritten with $\mathbf{u}=\mathbf{0}$, $k=\infty$, n=1 and $Q=1/K_f$. The undrained condition corresponds to $\mathbf{w}=0$ and k=0 in the above formulations.

COMPUTED RESULTS AND REMARKS

Effects of submerged conditions on the dynamic response of soil deposits are examined for a homogeneous soil profile shown in Fig. 1. The present formulation requires dividing the soil into multi-layers for computation. In the first study, however, only one layer is used in order to avoid complexity in the results and to see the essence of coupled behavior of solid skeleton and pore fluid. Fig. 2 shows wave number dispersion curves for various conditions. The imaginary and real parts of h define respectively the wave length and the rate of decay of Rayleigh waves according to e-ihx. The mode 1 and 2 denoted in the dispersion curves for dry soil are associated respectively with S-wave and P-wave. When the soil is dry, those mode 1 and mode 2 waves are not progressive at the frequencies below the natural frequency of the soil deposits associated respectively with Swave and P-wave. Above those natural frequencies, they are progressive to form waves in the x direction. When the condition is submerged and undrained, the high pore fluid stiffness increases the P-wave velocity and therefore the mode 2 wave does not propagate until the frequency substantially higher than that for dry soil. When this mode wave is not progressive, the displacements decay somewhat more quickly with distance than those for the dry condition. The pore fluid stiffness affects the S-wave velocity very little and therefore the natural frequecies of the soil associated S-waves. When the condition is submerged and drained, one additional mode exists in this case as seen in Figs. 2c and 2d because of the additional degree of the freedom due to the fluid motion. In the case k = 10-3 m/s, the first and second mode waves are very similar to those observed for the undrained condition, but the third mode wave is a progressive wave at any frequency and decays very quickly with x. As is seen in Fig. 3, the fluid motion relative to the solid

motion in the third mode is rather independent of permeability, whereas those in the other two modes decrease with decreasing permeability. When the relative fluid motions are large, a strong coupling develops between the pore fluid and soil skeleton. As a result, the dispersion curves associated with modes 1 and 2 are significantly affected by the coupling and thus the difference between the two types modes are not clear, as is seen for $k = 10^{-1}$ m/s case.

It is assumed that a vertical impermeable wall penetrates through the soil deposits at x = 0 and is subjected to either a vertical or lateral concentrated harmonic load at the location of the ground surface. For simplicity, the wall is assumed to be massless and completely flexible. Ground displacements caused by vibration of the wall are computed along the ground surface by using the above computed wave numbers and mode shapes and are shown in Fig. 4 for $\omega H/v_s = 2$. The horizontal and vertical motions are uncoupled with each other for dry soil with v = .25 and are governed respectively by the first mode and second mode waves. Therefore, according to the real and imaginary parts of h_s at $\omega H/v_s = 2$ in Fig. 2a, the vertical displacements monotonically decay with distance x because of no real part h_s in the first mode, whereas horizontal displacements form a wave pattern with the wave length defined by the real part of the first mode wave h_s. When the soil is submerged, the horizontal and vertical motions are coupled with each other even with v = 0.25 and thus both horizontal and vertical motions form a wave pattern in x as soon as the first mode wave propagates. The difference in the imaginary part of hs in the first mode wave between the dry and submerged conditions can be clearly seen in the difference in wave lengths along x. The amplitudes and phase shifts of the displacements of the wall are shown in Fig. 5a at various frequencies for dry soil and submerged soil in undrained condition. The first peaks are due to the first mode wave and are located around the fundamental natural frequency of the soil deposits associated with S-wave ($\omega H/v_s$ = $\pi/2$). The second peaks, clearly seen in z direction displacements, are due to the second mode wave and are located around the fundamental natural frequency of the soil deposits

associated with P-wave ($\omega H/v_p = \pi/2$ with $v_p^2 = (\lambda + 2G + \alpha 2Q)/p$). The difference in pore fluid rigidity affects not only the amplitudes of the response but the location of the second peak. It affects the location of the first peak vey little because of its association with the S-wave. The relative fluid motions generate damping and therefore suppress the peak as seen in Fig. 5b. As frequency increases, however, the relative fluid motions become smaller and the difference between the undrained and drained conditions diminishes. Contrary to this, when the motion becomes slow, there is enough time for pore fluid diffusion and thus the submerged soil behavior is closer to that of the dry soil as frequency decreases.

Now the soil responses to the wall motions are recomputed by dividing the soil into 10 layers (see Fig. 1), in order to see the distribution of responses along the depth. The computed amplitudes of displacements and pressures at the wall are shown respectively in Figs. 6 and 7 at $\omega H/vs = 2$ for various permeabilities of the soil. It is noted that, at the frequency considered, the displacement responses for $k = 10^{-1}$ m/s and 10^{-5} m/s are very little different respectively from the displacement responses for the dry case and the undrained case. The lower the permeability, the higher the pore fluid pressure is induced due to more difficulty in pore fluid diffusion. In addition, free drainage at the ground surface affects the distribution of pore fluid pressure giving further complexity in the porewater pressure in the soil. The pore fluid is far stiffer compared with the soil skeleton stiffness and thus the soil responses along the depth are affected by the difference in permeability as seen in Figs 6 and 7.

Three different conditions are considered as shown in Fig. 8, for a nonhomogeneous soil profile identical to that shown in Fig. 1: they include dry soil (case A), submerged soil with water level at the ground surface (case B) and submerged soil with water level above the ground surface (case C). The shear wave velocities of the inhomogeneous soil are defined so that its fundamental natural frequency is identical to that of the homogeneous soil. Similar to the previous study, a completely flexible

massless vertical wall is assumed to be inserted in the soil and is subjected to a lateral harmonic motion at the surface of the soil. Both the soil and the water above the soil is divided into 5 layers each for the computation. The computed displacement amplitudes of the wall are shown in Fig. 9 at the ground surface. Clear peaks can be observed around the fundamental natural frequency of the soil associated with the S-wave in all three cases. It is interesting to notice that one additional peak exists below this frequency when the water exists above the soil. The water body above the soil affects the soil response significantly and the submerged condition again reduces the response significantly.

CONCLUSIONS

A semi-analytical method is developed for a dynamic response analysis of a fluidsaturated porous medium. The method uses the finite element discretization only along depth and analytical form in the lateral direction. The method is found to be numerically very efficient for two-phase mixture problems. The pore fluid in the soil mass affects the dynamic response of the soil deposits by not simply increasing the stiffness of the soil but also by coupling the soil skeleton motions with pore fluid motions. All those effects are affected by the loading rate relative to the pore fluid diffusion rate, boundary conditions and stress gradient. The coupling effects are more predominant for soils with higher permeabilities. When the permeability is low, a mode wave transmitted primarily to the fluid is distinctly different from those primarily transmitted to the soil skeleton and decays very quickly with distance. Under the static and drained conditions, the submerged soil response is identical to the dry soil. Under the dynamic condition, however, the transient pore fluid redistribution depends on the rate of loading and permeability of the soil. The response of submerged soil is closer to the undrained conditions when the combination of those are less favorable for pore fluid movement. The larger the pore fluid motions relative to the soil skeleton are, the higher the damping generated. When the soil is submerged below the water table, the water above the soil deposits can affect the dynamic response of the soil significantly and thus has to be taken into account in the dynamic response analysis of submerged soil under the water.

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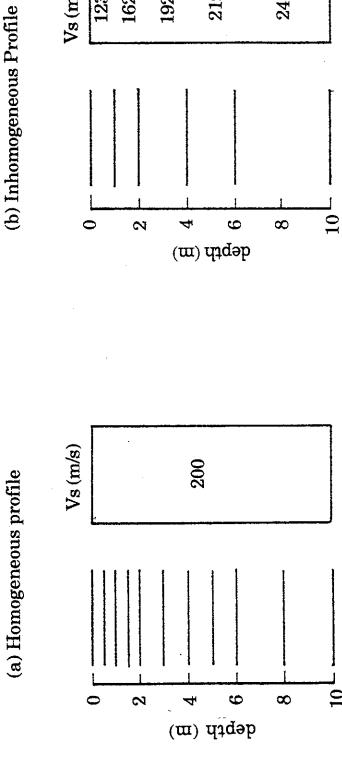
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Vs (m/s)



$$Ks = 3.7 \times 10^6 \ tf/m^2 \qquad Kf = 2.08 \times 10^5 \ tf/m^2$$

$$v = 0.25 \qquad D = 2 \%$$

$$n = 0.375 \qquad \gamma = 2.6 \ tf/m^3$$

Fig. 1 Homogeneous and inhomogeneous soil profiles



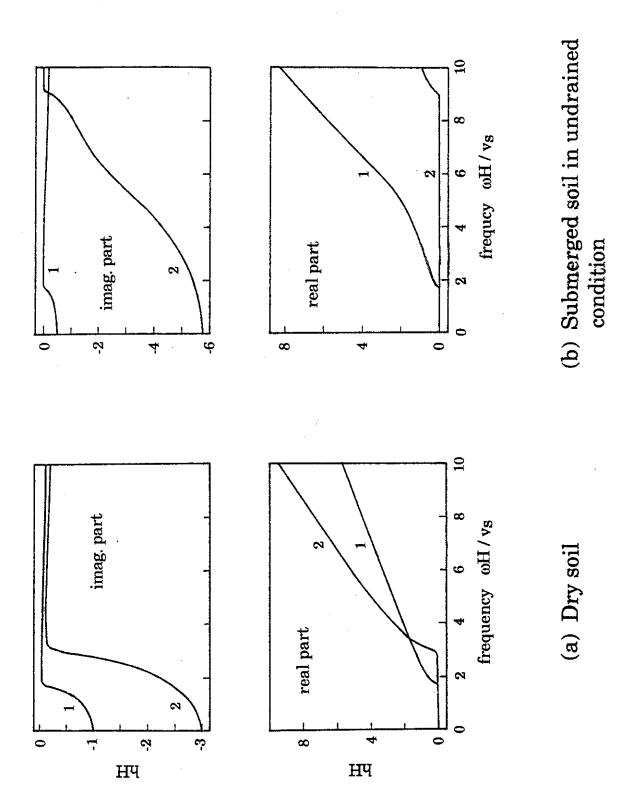


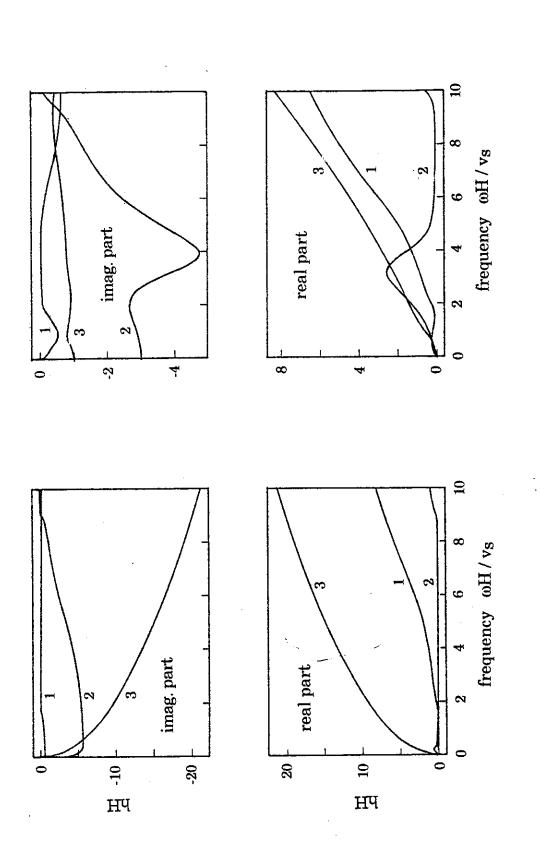
Fig. 2a, 2b Wave number dispersion curves

(d) Submerged soil in drained

(c) Submerged soil in drained

condition $(k = 10^{-3} \text{ m/s})$

condition $(k = 10^{-1} \text{ m/s})$



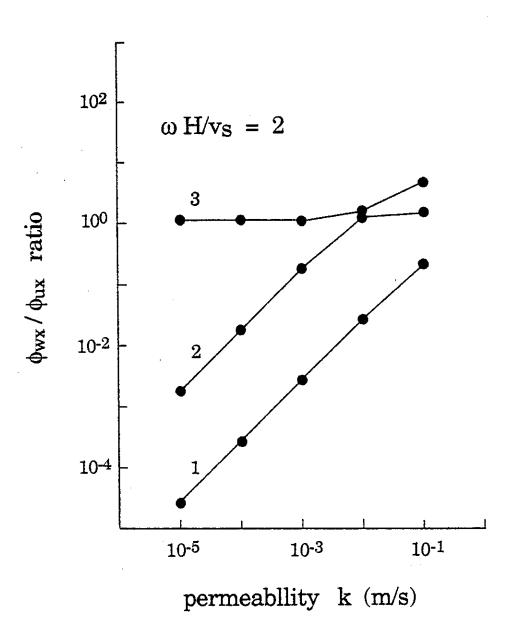
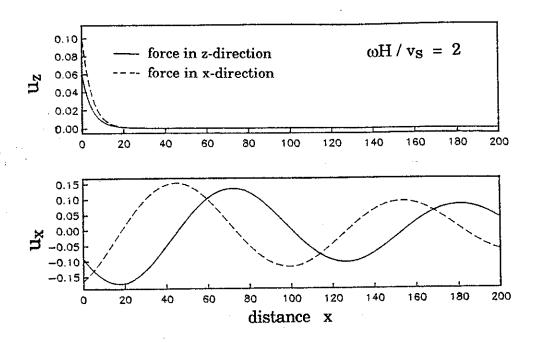
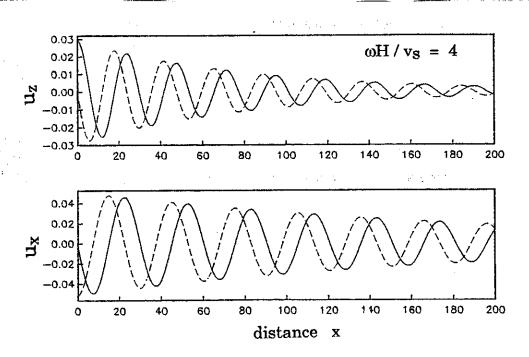


Fig. 3 Variation of ϕ_{wx} / ϕ_{ux} ratio with permeability

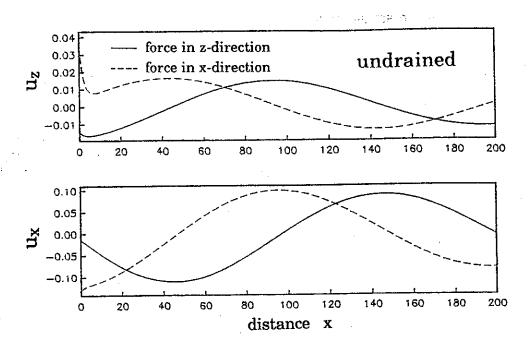


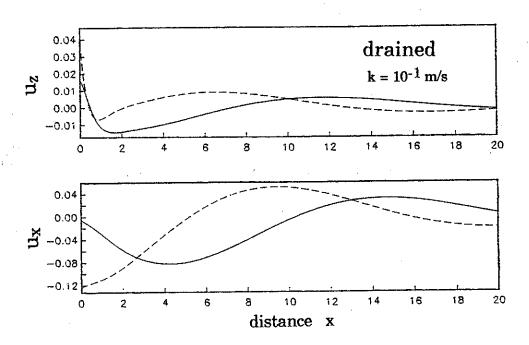




(a) Dry soil $(\omega H / v_S = 2 \text{ and } \omega H / v_S = 4)$

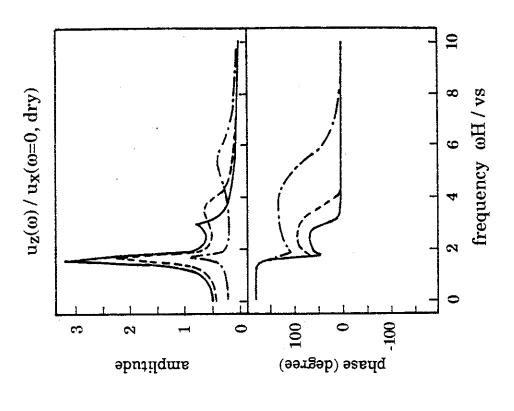
Fig. 4a Displacement amplitudes at various x along the ground surface

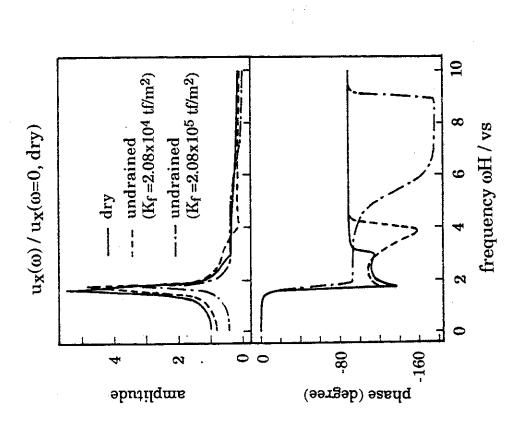




(b) Submerged soil in undrained and drained condition $(\omega H / v_S = 2)$

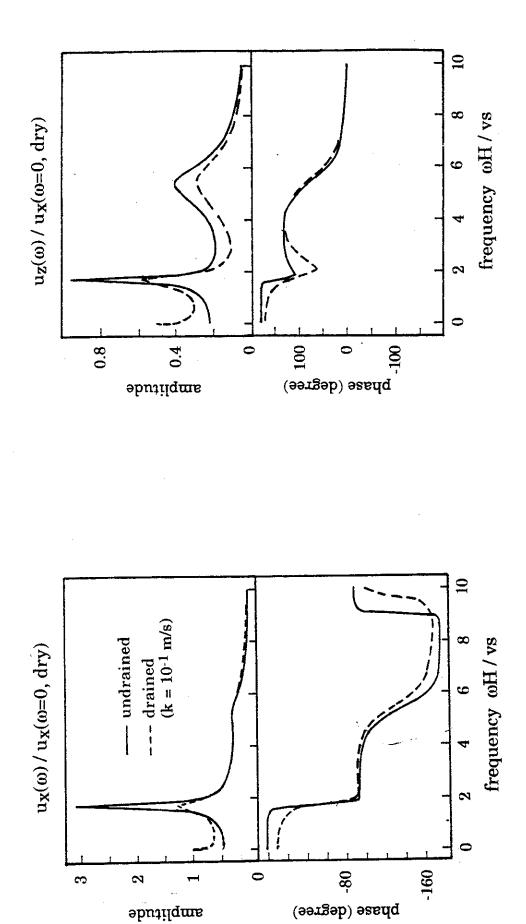
Fig. 4b Displacement amplitudes at various x along the ground surface





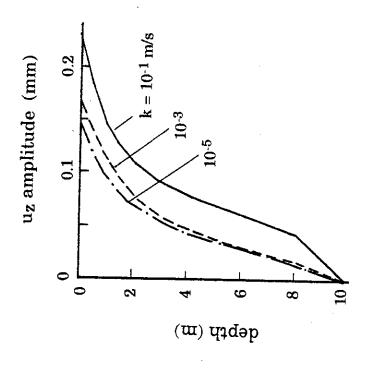
(a) dry soil and submerged soil in undrained conditon

Fig. 5a Displacements at the top of the vertical wall subjected to lateral vibration



(b) submerged soil in undrained and drained conditon

Fig. 5b Displacements at the top of the vertical wall subjected to lateral vibration



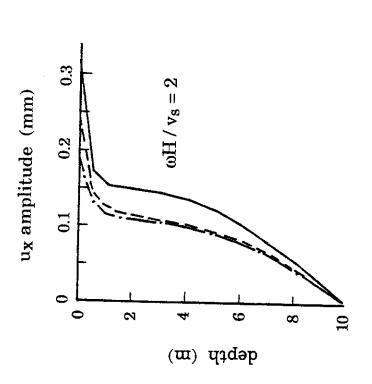


Fig. 6 Displacement response amplitudes of the wall along depth

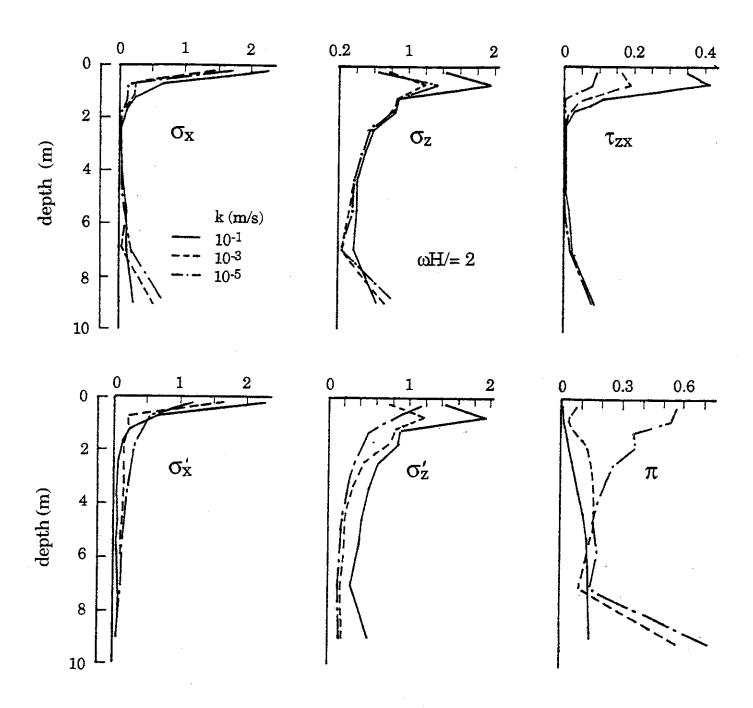
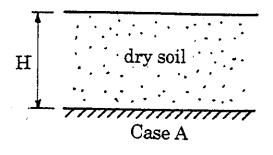
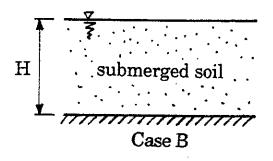


Fig. 7 Pressure response amplitudes at soil-wall interface along the wall





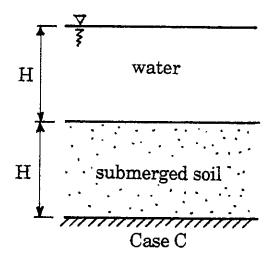
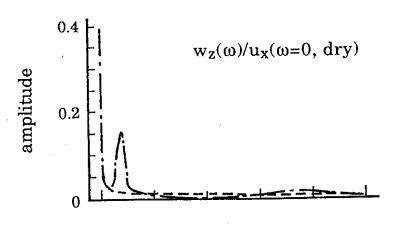
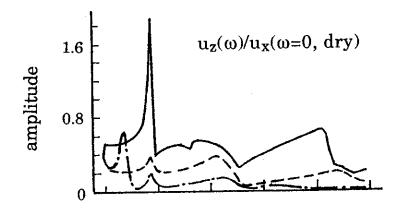


Fig. 8 Various cases considered for examples





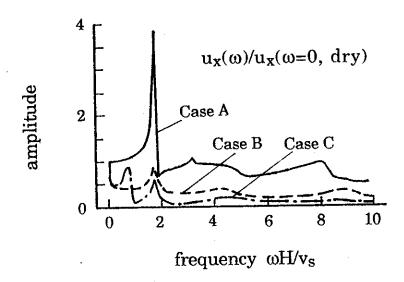


Fig. 9 Lateral displacement amplitudes at the top of the wall subjected to lateral vibration